## Loci \& Construction


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NOT TO
SCALE

The diagram shows a rectangular garden divided into different areas.
$F G$ is the perpendicular bisector of $B C$.
The arc $H J$ has centre $D$ and radius 20 m .
$C E$ is the bisector of angle $D C B$.
Write down two more statements using loci to describe the shaded region inside the garden.
The shaded region is

- nearer to $C$ than to $B$
- 

$11 A B C D$ is a rectangle with $A B=10 \mathrm{~cm}$ and $B C=6 \mathrm{~cm} . M N$ is the perpendicular bisector of $B C$. $A P$ is the bisector of angle $B A D$.
$O$ is the midpoint of $A B$ and also the centre of the semicircle, radius 5 cm .


Write the letter $R$ in the region which satisfies all three of the following conditions.

- nearer to $A B$ than to $A D$
- nearer to $C$ than to $B$
- less than 5 cm from $O$


Scale: 1 cm to 8 m

The rectangle $A B C D$ is a scale drawing of a rectangular football pitch.
The scale used is 1 centimetre to represent 8 metres.
(a) Construct the locus of points 40 m from $A$ and inside the rectangle.
(b) Using a straight edge and compasses only, construct the perpendicular bisector of $D B$.
(c) Shade the region on the football pitch which is more than 40 m from $A$ and nearer to $D$ than to $B$.

17 The diagram shows triangle $A B C$.

(a) Using a straight edge and compasses only, construct the bisector of angle $A B C$.
(b) Draw the locus of points inside the triangle that are 3 cm from $A C$.

20 The diagram shows the plan, $A B C D$, of a park. The scale is 1 centimetre represents 20 metres.


Scale: 1 cm to 20 m
(a) Find the actual distance $B C$.

> Answer(a)
m [2]
(b) A fountain, $F$, is to be placed

- 160 m from $C$
and
- equidistant from $A B$ and $A D$.

On the diagram, using a ruler and compasses only, construct and mark the position of $F$. Leave in all your construction lines.

Question 21 is printed on the next page.


The point $A$ lies on the circle centre $O$, radius 5 cm .
(a) Using a straight edge and compasses only, construct the perpendicular bisector of the line $O A$.
(b) The perpendicular bisector meets the circle at the points $C$ and $D$.

Measure and write down the size of the angle $A O D$.

$$
\begin{equation*}
\text { Answer(b) Angle } A O D= \tag{1}
\end{equation*}
$$


(a) On the diagram above, using a straight edge and compasses only, construct
(i) the bisector of angle $A B C$,
(ii) the locus of points which are equidistant from $A$ and from $B$.
(b) Shade the region inside the triangle which is nearer to $A$ than to $B$ and nearer to $A B$ than to $B C$.

(a) Construct the locus of all the points which are 3 cm from vertex $A$ and outside the rectangle. [2]
(b) Construct, using a straight edge and compasses only, one of the lines of symmetry of the rectangle.


For

The diagram shows a quadrilateral $A B C D$.
(a) Using a straight edge and compasses only, construct
(i) the perpendicular bisector of $A B$,
(ii) the bisector of angle $A D C$.
(b) Draw accurately the locus of points, inside the quadrilateral, that are 2 cm from $B C$.
(c) Shade the region, inside the quadrilateral, which is

> nearer to $B$ than to $A$
> and nearer to $D C$ than to $D A$
and more than 2 cm from $B C$.

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In the scale drawing, $P$ is a port, $L$ is a lighthouse and $S$ is a ship.
The scale is 2 centimetres represents 3 kilometres.
(a) Measure the bearing of $S$ from $P$.

> Answer(a)
(b) Find the actual distance of $S$ from $L$.
(c) The bearing of $L$ from $S$ is $160^{\circ}$.

Calculate the bearing of $S$ from $L$.
(d) Work out the scale of the map in the form $1: n$.
(e) A boat $B$ is

- equidistant from $S$ and $L$
and
- equidistant from the lines $P S$ and $S L$.

On the diagram, using a straight edge and compasses only, construct the position of $B$.
(f) The lighthouse stands on an island of area $1.5 \mathrm{~cm}^{2}$ on the scale drawing. Work out the actual area of the island.
(a) Draw accurately the locus of points, inside the quadrilateral $A B C D$, which are 6 cm from the point $D$.
(b) Using a straight edge and compasses only, construct
(i) the perpendicular bisector of $A B$,
(ii) the locus of points, inside the quadrilateral, which are equidistant from $A B$ and from $B C$. [2]
(c) The point $Q$ is equidistant from $A$ and from $B$ and equidistant from $A B$ and from $B C$.
(i) Label the point $Q$ on the diagram.
(ii) Measure the distance of $Q$ from the line $A B$.

> Answer(c)(ii)
(d) On the diagram, shade the region inside the quadrilateral which is

- less than 6 cm from $D$
and
- $\quad$ nearer to $A$ than to $B$
and
- nearer to $A B$ than to $B C$.

